

# Geometry

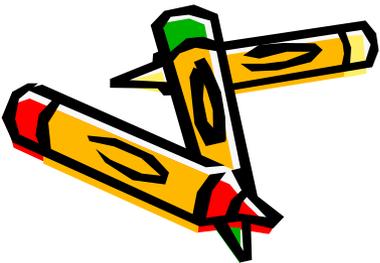
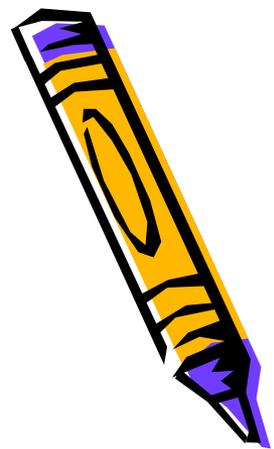
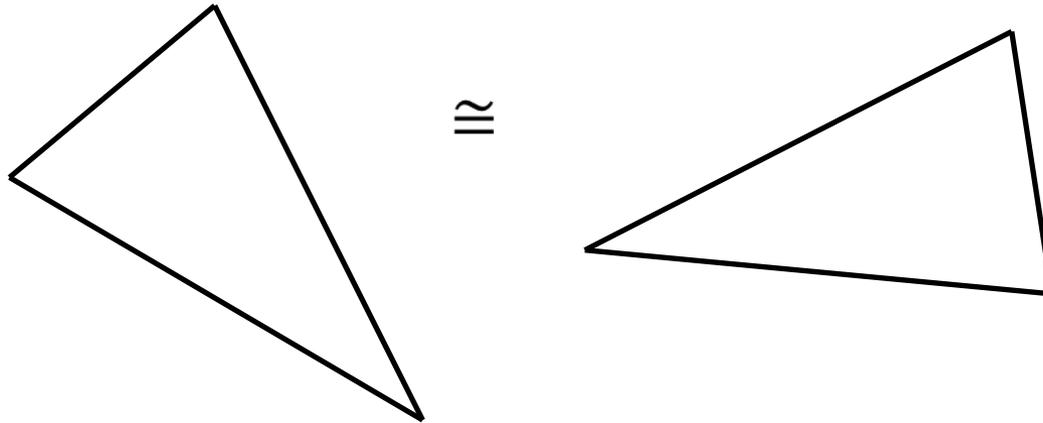
Exploring Congruent Triangles



# Vocabulary

- Congruent ( $\cong$ ): same shape, same size

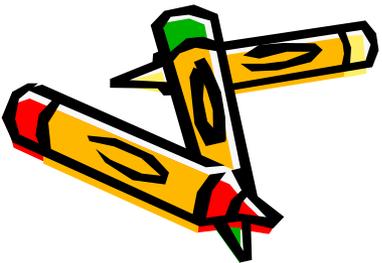
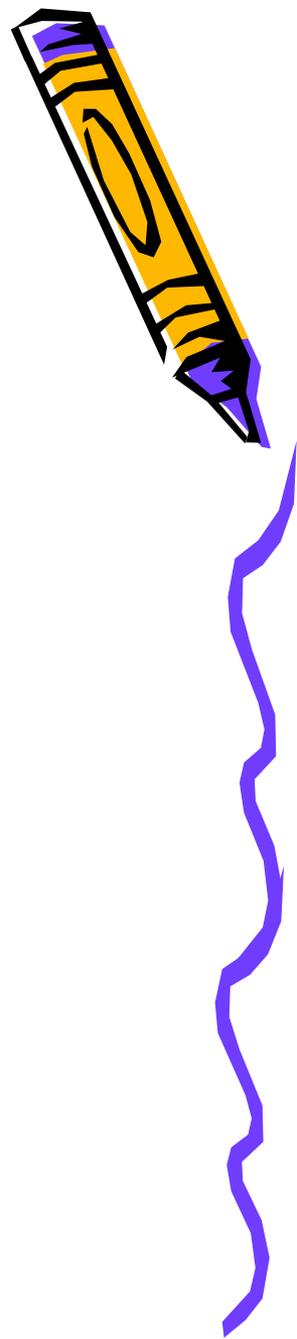
Congruence is not effected by translation, rotation, or reflection



# Vocabulary

- Congruent Triangles:  
Two triangles are congruent if and only if their corresponding parts are congruent
- CPCTC:  
Corresponding Parts of Congruent  
Triangles are Congruent

These statements are used interchangeably



# CPCTC

When writing congruence statements, it is important to name the letters of the vertices in corresponding order.

$$\triangle ABC \cong \triangle QRS$$

Vertex A corresponds to Vertex Q

Vertex B corresponds to Vertex R

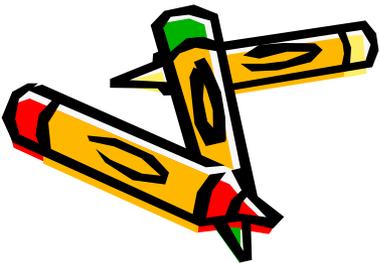
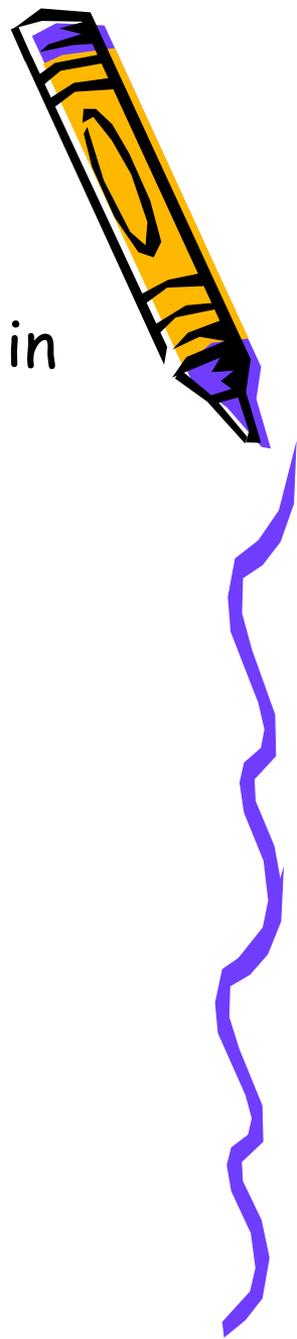
Vertex C corresponds to Vertex S

$$A \leftrightarrow Q$$

$$B \leftrightarrow R$$

$$C \leftrightarrow S$$

$\leftrightarrow$  means "corresponds to"



# CPCTC

Therefore...given,

$$\triangle ABC \cong \triangle QRS$$

$$\angle A \leftrightarrow \angle Q$$

$$\angle B \leftrightarrow \angle R$$

$$\angle C \leftrightarrow \angle S$$

$$\overline{AB} \leftrightarrow \overline{QR}$$

$$\overline{BC} \leftrightarrow \overline{RS}$$

$$\overline{AC} \leftrightarrow \overline{QS}$$

AND

$$\angle A \cong \angle Q$$

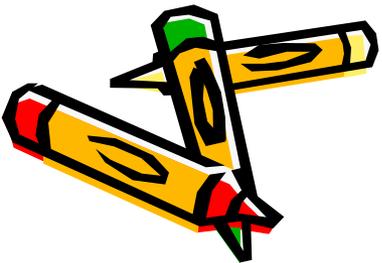
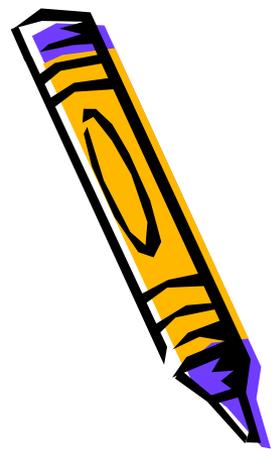
$$\angle B \cong \angle R$$

$$\angle C \cong \angle S$$

$$\overline{AB} \cong \overline{QR}$$

$$\overline{BC} \cong \overline{RS}$$

$$\overline{AC} \cong \overline{QS}$$



# CPCTC

When writing congruence statements, it is important to name the letters of the vertices in corresponding order.



Name the first triangle however you choose, but the second must be in corresponding order.

$$\triangle ABC \cong \triangle QRS$$

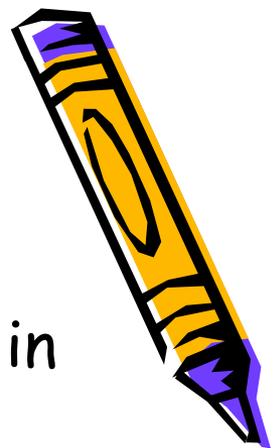
$$\triangle ACB \cong \triangle QSR$$

$$\triangle BAC \cong \triangle RQS$$

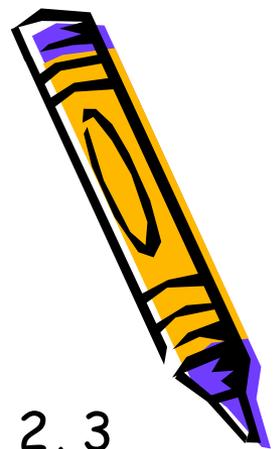
$$\triangle BCA \cong \triangle RSQ$$

$$\triangle CAB \cong \triangle SQR$$

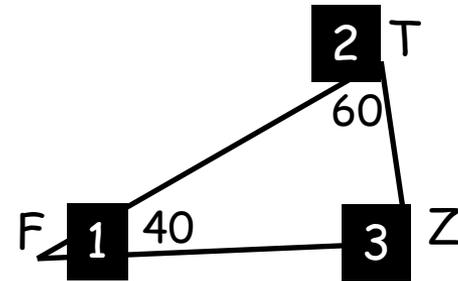
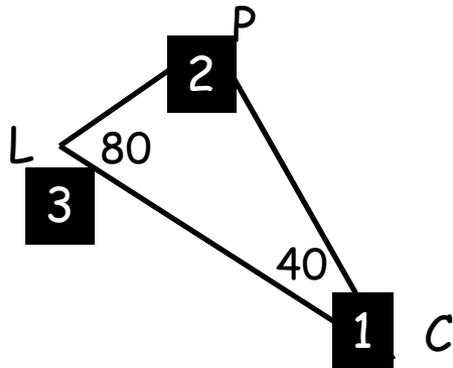
$$\triangle CBA \cong \triangle SRQ$$



# Congruence Statements Strategy



Mark off the congruent / corresponding angle pairs as: 1, 2, 3



Use this to name things in corresponding order:

The side that goes from  $\sphericalangle 1$  to  $\sphericalangle 2$

$$\begin{array}{l} \overline{CP} \cong \overline{FT} \\ \overline{LC} \cong \overline{ZF} \end{array}$$

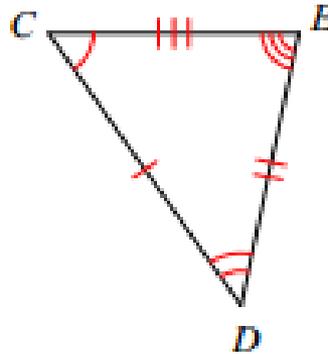
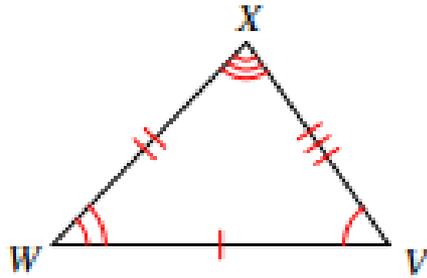
$$\begin{array}{l} \sphericalangle PCL \cong \sphericalangle TFZ \\ \sphericalangle CLP \cong \sphericalangle FZT \end{array}$$

Note the order of the letters. It follows the pattern: 213



# Congruence Statements

Complete each congruence statement:



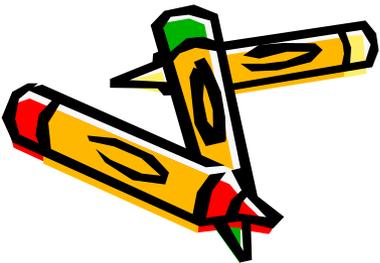
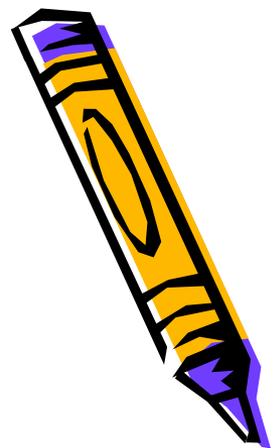
1.  $\overline{WV} \cong$  \_\_\_\_\_

2.  $\angle ECD \cong$  \_\_\_\_\_

3.  $\overline{EC} \cong$  \_\_\_\_\_

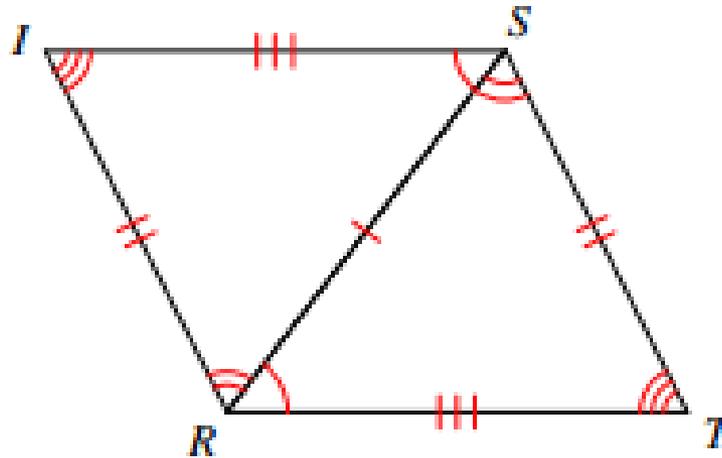
4.  $\angle VWX \cong$  \_\_\_\_\_

5.  $\triangle XVW \cong$  \_\_\_\_\_



# Congruence Statements

Complete each congruence statement:



1.  $\overline{ST} \cong$  \_\_\_\_\_

2.  $\angle ISR \cong$  \_\_\_\_\_

3.  $\overline{SI} \cong$  \_\_\_\_\_

4.  $\angle RST \cong$  \_\_\_\_\_

5.  $\triangle STR \cong$  \_\_\_\_\_

