

BD, AF, and EC are medians with G as the centroid of the triangle. For each question, find x.

18. $CG = 3x + 7$ and $CE = 6x$

19. $FG = x + 8$ and $AF = 9x - 6$

20. $BG = 5x - 1$ and $DG = 4x - 5$

$BG = 2(DG)$

$5x - 1 = 2(4x - 5)$

$5x - 1 = 8x - 10$

$9 = 3x$

$3 = x$

$CG = \frac{2}{3} CE$

$FG = \frac{2}{3} AF$

$(x+8) = \frac{2}{3}(9x-6)$

$x+8 = 3x-2$

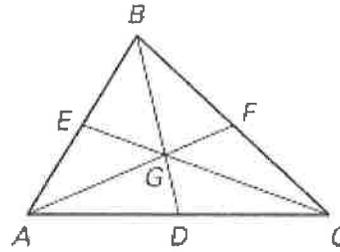
$10 = 2x$

$5 = x$

$(3x+7) = \frac{2}{3}(6x)$

$3x+7 = 4x$

$7 = x$



In the figure E, F, and D are the midpoints of their respective sides.

21. Given that $AB=CB$, find AD and $\angle ABD$

22. Find GD and BD

12 39
 $GD = 5$ BY PYTHAG

$BD = 14.8$ BY TRIG

23. Name a median $\overline{AF}, \overline{CE}, \overline{BD}$

24. Name an angle bisector \overline{BD}

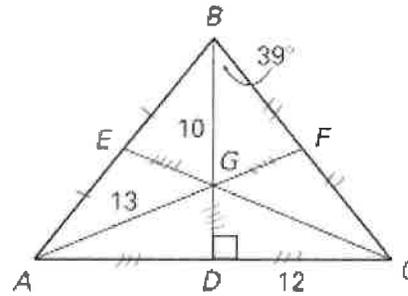
25. Name a perpendicular bisector \overline{BD}

26. Find EF 12

27. $AD = 2x - 4$. Find x .

$2x - 4 = 12$

$x = 8$

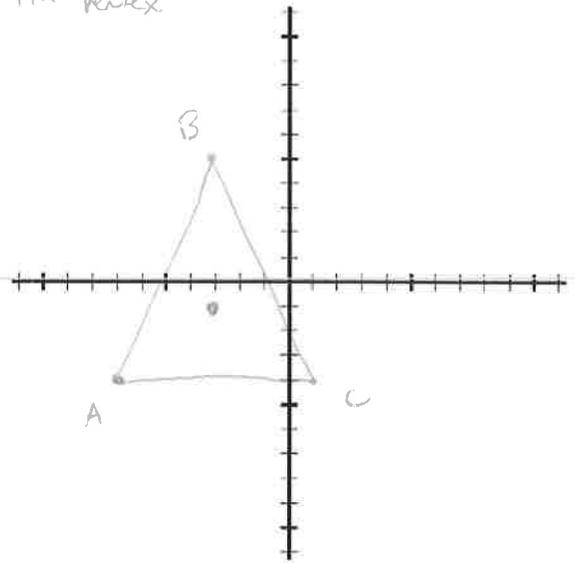


Find the coordinates of the centroid P for each triangle.

$\frac{2}{3}$ of way along medians from THE vertex
 RECALL Partitioning A Directed Line Segment

1. $A(-7, -4), B(-3, 5), C(1, -4)$

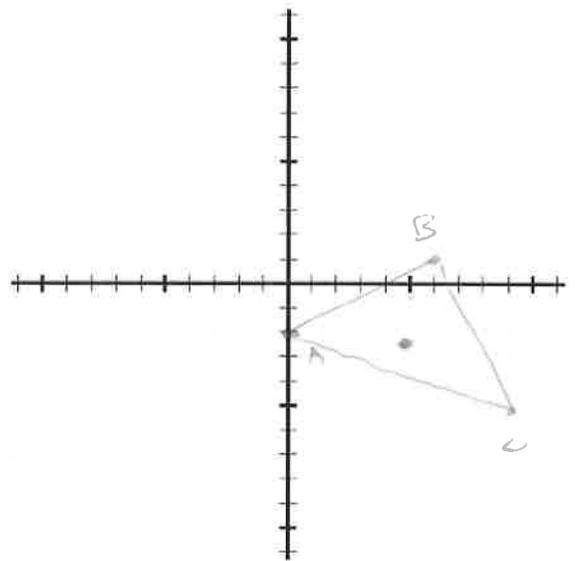
① Find medians endpoint
 for example \overline{BM} , find M
 $m = (-3, -4)$



② Partition \overline{BM} $\frac{2}{3}$ of THE way
 Run = 0 Times $\frac{2}{3} = 0$ $-3 + 0 = -3$
 Rise = -9 Times $\frac{2}{3} = -6$ $5 + -6 = -1$
 CENTROID AT $(-3, -1)$

2. $A(0, -2), B(6, 1), C(9, -5)$

$\overline{BM} \rightarrow m(4.5, -3.5)$



$\frac{2}{3}$ of way $B \rightarrow m$
 Run = 1.5 Times $\frac{2}{3} = 1$ $6 + 1 = 7$
 Rise = -4.5 Times $\frac{2}{3} = -3$ $1 + -3 = -2$
 CENTROID $(7, -2)$

G is the centroid of $\triangle ABC$, $AD = 8$, $AG = 10$, and $CD = 18$. Find the length of the segment.

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|-----------------------|-----------------------|
| 1. \overline{BD} 8 | 2. \overline{AB} 16 |
| 3. \overline{EG} 5 | 4. \overline{AE} 15 |
| 5. \overline{CG} 12 | 6. \overline{DG} 6 |

